## The Surprising Versatility of Edge-Matching Tiles



## MiniMatch-I <br> 9 edge-colored squares



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## Research Results:

## 1. Enclose any one color



## 2. Enclose two colors.

Only purple/white and red/white are solvable.


## 3. Wrap-arounds.

- Cylinder
- Torus
- Moebius Strip
- Klein Bottle
- Projective Plane



## 4. Wrap-around transformations.

After shifting one row from top to bottom:


## 5. Unmatched row ends. Very difficult.



## 6. Interior color divisions.

12 interior color squares can contain 3 or 4 colors in all these different sums:

$$
\begin{array}{llllll}
5430 & 5421 & 5331 & 5322 & 4440 \\
4431 & 4422 & 4332 & 3333 &
\end{array}
$$

The only combinations with no solutions are 552 and 5511


## 7. Other observations.

- Only one of the four colors can be entirely on the border.
- Can form 78 other color-matched symmetrical shapes. Here's one.
- Can form perfect mirror symmetry of all colors, producing double wrap-arounds as well.



## 8. Non-matching arrangements.

A liberating, artistic exercise...


## 9. Mega-constructions

Any single $3 \times 3$ solution can tile infinitely-on floors, walls, as art.


## There is no end!

## www.gamepuzzles.com

